Känguru der Mathematik 2019 Level Junior (Schulstufe 9 and 10) Austria – 21. 3. 2019





- 4 Point Examples -

11.	Three five-digit numbers are written onto three separate pieces of paper as shown. Three of the digits in the picture are hidden. The sum of the three numbers is 57263. Which are the hidden digits?					
	(A) 0, 2 and 2	(B) 1, 2 and 9	(C) 2, 4 and 9	(D) 2, 7 and 8	(E) 5, 7 and 8	
12.	 Anna, Bella, Claire, Dora, Erika and Frieda meet at a party. Each pair who know each other shake hands exactly once. Anna shakes hands only once, Bella twice, Claire three times, Dora four times and Erika five times. How many people does Frieda shake hands with? (A) 1 (B) 2 (C) 3 (D) 4 (E) 5 					
4.2		(B) Z				
13.	whose vertices of whose vertice How big is the	s are also labelled angle CBE?	d anti-clockwise	-ciockwise. A an	d C are the vertices of a	an equilateral triangle AEC,
	(A) 30°	(B) 45°	(C) 135°	(D) 145°	(E) 150°	
14.	The numbers a , b , c and d are pairwise different integers between 1 and 10 (1 and 10 including). What is the smallest possible value of the expression $\frac{a}{b} + \frac{c}{d}$?					
	(A) $\frac{2}{10}$	(B) $\frac{3}{19}$	(C) $\frac{14}{45}$	(D) $\frac{29}{90}$	(E) $\frac{25}{72}$	
15.	 The flag of Kanguria is a rectangle whose side lengths are in the ratio 3: 5. The flag is split into four rectangles of equal area as shown. In which ratio are the side lengths of the white rectangle? 					
	(A) 1:3	(B) 1:4	(C) 2:7	(D) 3:10	(E) 4:15	
16.	16. A 3 × 2 rectangle can be covered in two ways by two of the L-shaped figures as shown:					
	In how many	ways can the dia	gram on the righ	nt be covered by	these L-shaped figures	5?
	(A) 1	(B) 2	(C) 3	(D) 4	(E) 48	
17.	A triathlon con entire distance long is the wh (A) 10	nsists of three dis e, the running roo ole distance of th (B) 20	ciplines swimmi ute is one fifth o ne triathlon in kn (C) 38	ing, running and f the entire dista n? (D) 40	cycling. The cycle route ance and the swimming (E) 60	e is three quarters of the g route is 2 km long. How
18. A 1-liter-bottle of syrup is still half full. The syrup shall be diluted in the ratio 1: 7 to make juice. Which fraction of the syrup should be used to obtain 2 litres of juice?						
	(A) $\frac{1}{4}$	(B) $\frac{1}{2}$	(C) $\frac{2}{7}$	(D) $\frac{4}{7}$	(E) the whole syrup	
19.	9. The diagram consists of three circles of equal radius <i>R</i> . The centre of those circles lie on a common straight line where the middle circle goes through the centres of the other two circles (see diagram). How big is the perimeter of the figure?					
	(A) $\frac{10\pi R}{3}$	(B) $\frac{5\pi R}{3}$	(C) $\frac{2\pi R\sqrt{3}}{3}$	(D) $2\pi R\sqrt{3}$	(E) 4 <i>π R</i>	
20.	• The sum of the seven digits of a seven-digit phone number $aaabbbb$ is a two-digit number ab . How big is the value of the sum $a + b$?					
	(A) 8	(B) 9	(C) 10	(D) 11	(E) 12	

- 5 Point Examples -

21. If one of the digits of a two-digit number is deleted, the result in both cases is a factor of the original number. How many two-digit numbers have this property?

(A) 5 (B) 9 (C) 14 (D) 19 (E) 23

22. 60 apples and 60 pears in total are shared out in several boxes. There should be the same amount of apples in each box but no two boxes should contain the same amount of pears. Each box contains both fruits. What is the maximum number of boxes that can be filled in this way?



30. What is the minimum number of elements of the set {10, 20, 30, 40, 50, 60, 70, 80, 90} that have to be removed so that the product of the remaining elements of the set is a square number?

(A) 1 (B) 2 (C) 3 (D) 4 (E) 5